

Using Frama-C

Frama-C 29.0

Coq 8.15.2

Alt-ergo 2.4.2

Frama-C

- A suite of tools for the analysis of source code written in C
 - A modified version of CIL (C Intermediate Language) as the kernel
 - Static and dynamic analysis techniques
 - Extensible architecture
 - Collaborations across analyzers
 - Bug free versus bug finding

A Simple Program

```
int abs(int x) {  
    if (x < 0) return -x;  
    else return x;  
}
```

abs.c

Is this program correct?

A Simple Program

```
int abs(int x) {  
    if (x < 0) return -x;  
    else return x;  
}
```

abs.c

Is this program correct? **No**

Range of 32-bit int: $[-2^{31}, 2^{31} - 1]$

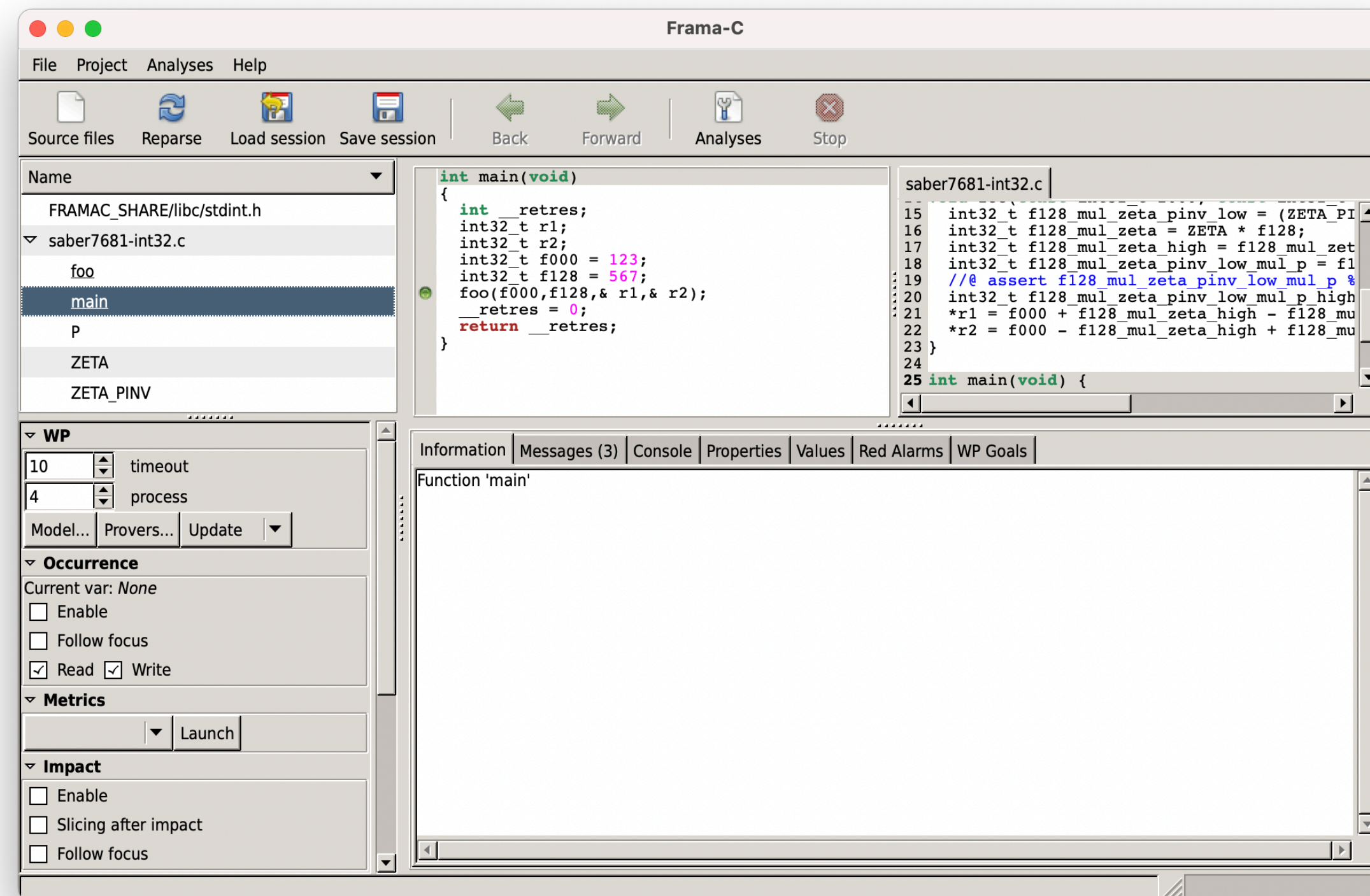
Installation

- Installation instructions: <https://frama-c.com/html/get-frama-c.html>
- It is recommended to install Frama-C via **opam** (<https://opam.ocaml.org>)
 - frama-c
 - why3
 - why3-coq
 - coq
 - coqide
 - alt-ergo

Basic Usage

\$ frama-c -PLUGIN -OPTION₁ -OPTION₂ ... file.c -OPTION_i ...

\$ frama-c-gui -PLUGIN -OPTION₁ -OPTION₂ ... file.c -OPTION_i ...



Action Order

- Actions are applied in order according to **-then**.
 - \$ frama-c ARGS-ACT-1 -then ARGS-ACT-2 -then ARGS-ACT-3 ...
- The action after **-then-on PROJECT** is applied after PROJECT
- The action specified after **-then-last** is applied on the last project created by a program transformer

Value Analysis via EVA

- Based on **abstract interpretation**
- Compute variation domains for variables
- Can detect runtime errors such as overflow problems
- Byproducts:
 - Possible ranges of values and addresses for variables
 - Code reachability
 - Call graphs
- Recursive calls are not supported

EVA Example 1

```
int dbl(int n) {
    return n * 2;
}

int main(void) {
    int n, m = 0;
    printf("Enter an integer: ");
    scanf("%d", &n);
    if (0 <= n && n <= 3)
        m = dbl(n);
    return 0;
}
```

dbl-1.c

\$ frama-c -eva dbl-1.c

...
[eva:final-states] Values at end of function main:
 $n \in [---...---]$
 $m \in \{0; 2; 4; 6\}$
 $_retres \in \{0\}$
 $S_fc_stdin[0..1] \in [---...---]$
 $S_fc_stdout[0..1] \in [---...---]$
[eva:summary] ===== ANALYSIS SUMMARY =====

...

[---...---]: the set of all integers that fit within the type of the variable or expression

EVA Example 2

-Wider Range-

```
int dbl(int n) {
    return n * 2;
}

int main(void) {
    int n, m = 0;
    printf("Enter an integer: ");
    scanf("%d", &n);
    if (0 <= n && n <= 9)
        m = dbl(n);
    return 0;
}
```

dbl-2.c

[eva:final-states] Values at end of function dbl:

$_retres \in [0..18], 0\%2$

[eva:final-states] Values at end of function main:

$n \in [---..---]$

$m \in [0..18], 0\%2$

$_retres \in \{0\}$

...

[L..H]: $\{ n \mid L \leq n \leq H \}$

[L..H],r%m: $\{ n \mid L \leq n \leq H, \text{ and } n \% m = r \}$

-eva-ilevel <n>: controls the maximal number of integers that should be precisely represented as a set

EVA Example 3

-Loops-

```
int main(void) {  
    int x = 0, y = 1;  
    for (int i = 0; i < 10; i++) {  
        int tmp = x;  
        x = y;  
        y = tmp + 2 * y;  
    }  
    int a = x;  
    int b = y;  
    return 0;  
}
```

dbl-3.c

[eva:final-states] Values at end of function main:

$x \in [0..2147483647]$

$y \in [1..2147483647]$

$a \in [0..2147483647]$

$b \in [1..2147483647]$

$_retres \in \{0\}$

...

EVA Example 4

-Precision Improvement-

```
int main(void) {  
    int x = 0, y = 1;  
    //@ loop unroll 10;  
    for (int i = 0; i < 10; i++) {  
        int tmp = x;  
        x = y;  
        y = tmp + 2 * y;  
    }  
    int a = x;  
    int b = y;  
    return 0;  
}
```

dbl-4.c

[eva:final-states] Values at end of function main:

$x \in \{2378\}$

$y \in \{5741\}$

$a \in \{2378\}$

$b \in \{5741\}$

$_retres \in \{0\}$

...

-eva-auto-loop-unroll <n>: loops with less than <n> iterations will be completely unrolled

-eva-min-loop-unroll <n>: specify the number of iterations to unroll in each loop

Catch Overflow Bugs

abs.c

```
int abs(int x) {  
    if (x < 0) return -x;  
    else return x;  
}
```

Range of 32-bit int: $[-2^{31}, 2^{31} - 1]$
 $2^{31} = 2147483648$

```
$ frama-c -eva -main abs abs.c
```

```
[kernel] Parsing abs.c (with preprocessing)
```

```
[eva] Analyzing a complete application starting at abs
```

```
[eva:initial-state] Values of globals at initialization
```

```
[eva:alarm] abs.c:5: Warning: signed overflow. assert -x ≤ 2147483647;
```

```
[eva] ===== VALUES COMPUTED =====
```

```
[eva:final-states] Values at end of function abs:
```

```
  _retres ∈ [0..2147483647]
```

```
[eva:summary] ===== ANALYSIS SUMMARY =====
```

```
...
```

False Alarms

```
#define MAX 100

int compute_next(int x) {
    return (x % 2 == 0) ?
        x / 2 : 3*x + 1;
}

void collatz(int n) {
    int t[MAX];
    t[0] = n;
    for (int i = 0; i < MAX; i++) {
        t[i + 1] = compute_next(t[i]);
    }
}
```

```
$ frama-c -eva -main collatz collatz.c
```

```
...
```

```
[eva:summary] ===== ANALYSIS SUMMARY =====
```

```
-----  
2 functions analyzed (out of 2): 100% coverage.
```

```
In these functions, 12 statements reached (out of 14): 85% coverage.
```

```
-----  
No errors or warnings raised during the analysis.
```

```
-----  
4 alarms generated by the analysis:
```

```
    2 integer overflows
```

```
    1 access out of bounds index
```

```
    1 access to uninitialized left-values
```

```
-----  
No logical properties have been reached by the analysis.
```

Example from Guide to Software Verification with Frama-C

False Alarms (cont'd)

```
3 #define MAX 100
5 int compute_next(int x) {
6     return (x % 2 == 0) ?
7         x / 2 : 3*x + 1;
9 void collatz(int n) {
10    int t[MAX];
11    t[0] = n;
12    for (int i = 0; i < MAX; i++) {
13        t[i + 1] = compute_next(t[i]);
14    }
15}
```

```
$ frama-c -eva -main collatz collatz.c
...
[eva:alarm] collatz.c:6: Warning: signed overflow.
assert -2147483648 ≤ 3 * x;
[eva:alarm] collatz.c:6: Warning: signed overflow.
assert 3 * x ≤ 2147483647;
[eva] collatz.c:12: starting to merge loop iterations
[eva:alarm] collatz.c:13: Warning:
    accessing uninitialized left-value. assert
    \initialized(&t[i]);
[eva:alarm] collatz.c:13: Warning:
    accessing out of bounds index. assert (int)(i + 1) <
    100;
...
[eva:summary] ===== ANALYSIS SUMMARY =====
...
```

Example from Guide to Software Verification with Frama-C

A Corrected Version

```
#include <limits.h>
#define MAX 100

int compute_next(int x) {
    return (x % 2 == 0) ? x / 2 : 3*x + 1;
}

int collatz(int n) {
    int i, t[MAX];
    t[0] = n;
    if (n < 0) return -1;
    for (i = 0; i < MAX - 1; i++) {
        int v = t[i];
        if (v > INT_MAX / 3) return -1;
        t[i + 1] = compute_next(v);
    }
    return i;
}
```

Example from Guide to Software Verification with Frama-C with one modification

```
$ frama-c -eva -main collatz collatz-corrected.c
```

```
...
```

```
-----
2 alarms generated by the analysis:
```

```
1 integer overflow
```

```
1 access to uninitialized left-values
```

```
-----
No logical properties have been reached by the analysis.
-----
```

There are still false alarms

⇒ We need to increase the precision of EVA

Increase EVA Prevision

```
#include <limits.h>
#define MAX 100

int compute_next(int x) {
    return (x % 2 == 0) ? x / 2 : 3*x + 1;
}

int collatz(int n) {
    int i, t[MAX];
    t[0] = n;
    if (n < 0) return -1;
    for (i = 0; i < MAX - 1; i++) {
        int v = t[i];
        if (v > INT_MAX / 3) return -1;
        t[i + 1] = compute_next(v);
    }
    return i;
}
```

Example from Guide to Software Verification with Frama-C with one modification

```
$ frama-c -eva -main collatz -eva-precision 5 collatz-corrected.c
```

...

No errors or warnings raised during the analysis.

0 alarms generated by the analysis.

No logical properties have been reached by the analysis.

-eva-precision <N>: <N> from 0 to 11

Limitations: Recursive Functions

```
int loop(int x) {  
    if (x < 0)  
        return loop(x + 1);  
    else if (x > 0)  
        return loop(x - 1);  
    else  
        return 0;  
}
```

```
$ frama-c -eva -eva-precision 11 -main loop eva-limitations-1.c
```

```
...
```

```
[eva:final-states] Values at end of function loop:
```

```
  _retres ∈ [---...---]
```

```
...
```

The function loop always returns 0

The result of EVA can be further improved with proper ACSL specifications

Limitations: Value Domains

```
int divi(int x, int y) {  
    if (y > 10000) return 0;  
    if (y < -10000) return 0;  
    if (x > 10000) return 0;  
    if (x < -10000) return 0;  
    if (y != 0) return x / y;  
    return 0;  
}
```

The abstract domain $[-10000, 10000]$ of y after $y \neq 0$ is still $[-10000, 10000]$

This can be improved by case splitting

```
$ frama-c -eva -eva-precision 11 -main divi eva-limitations-2.c
```

```
...
```

```
[eva:final-states] Values at end of function divi:
```

```
  _retres  $\in [-10000..10000]$ 
```

```
[eva:summary] ===== ANALYSIS SUMMARY =====
```

```
-----
```

```
1 function analyzed (out of 1): 100% coverage.
```

```
In this function, 22 statements reached (out of 22): 100% coverage.
```

```
-----
```

```
No errors or warnings raised during the analysis.
```

```
-----
```

```
1 alarm generated by the analysis:
```

```
  1 division by zero
```

```
-----
```

```
No logical properties have been reached by the analysis.
```

```
-----
```

Limitations: Value Domains (cont'd)

```
int divi(int x, int y) {
    if (y > 10000) return 0;
    if (y < -10000) return 0;
    if (x > 10000) return 0;
    if (x < -10000) return 0;
    //@ split y >= 0;
    if (y != 0) return x / y;
    return 0;
}
```

Split into two cases by `//@ split e;`

- `e` is satisfied \Rightarrow in this case, `[0, 10000]`
- `e` is violated \Rightarrow in this case, `[-10000, -1]`

```
$ frama-c -eva -eva-precision 11 -main divi eva-limitations-3.c
```

```
...
```

```
[eva:summary] ===== ANALYSIS SUMMARY =====
```

```
-----  
1 function analyzed (out of 1): 100% coverage.
```

```
In this function, 23 statements reached (out of 23): 100% coverage.
```

```
-----  
No errors or warnings raised during the analysis.
```

```
-----  
0 alarms generated by the analysis.
```

```
-----  
No logical properties have been reached by the analysis.
```

Runtime Assertions via E-ACSL

- E-ACSL is used for runtime annotation checking (RAC)
- Translate an annotated C program into another program with runtime assertions
 - Both programs have the same behavior if no annotation is violated
- Possible usage:
 - Detect undefined behaviors (+RTE)
 - Verification of linear temporal properties (+Aoraï)
 - Verification of security properties (+SecureFlow)

E-ACSL Example 1

```
/*@
  @ ensures x <= \result && y <= \result;
  @ ensures \result == x || \result == y;
  @*/
int max(int x, int y) {
  if (x < y) return y;
  else return x;
}

int main(void) {
  int x, y, z;
  z = max(x, y);
  return 0;
}
```

max.c

\$ frama-c -e-acsl max.c -then-last -print

E-ACSL Example 1

```
/*@
int __gen_e_acsl_max(int x, int y) result;
{
  int __gen_e_acsl_at_2;
  int __gen_e_acsl_at;
  int __retres;
  __gen_e_acsl_at = x;
  __gen_e_acsl_at_2 = y;
  __retres = max(x,y);
  {
    ..
  }
}
return 0;
}
```

max.c

```
$ frama-c -e-acsl max.c -then-last -print
```

Every call to max is replaced by a call to __gen_e_acsl_max.

E-ACSL Example 1

```
/*@
int __gen_e_acsl_max(int
{
  int __gen_e_acsl_at_2;
  int __gen_e_acsl_at;
  int __retres;
  __gen_e_acsl_at = x;
  __gen_e_acsl_at_2 = y;
  __retres = max(x,y);
  {
  ...
  }
}

return 0;
}

int __gen_e_acsl_and;
int __gen_e_acsl_or;
__e_acsl_assert_data_t __gen_e_acsl_assert_data = {.values = (void *)0};
__e_acsl_assert_register_int(& __gen_e_acsl_assert_data, "\\old(x)", 0,
                             __gen_e_acsl_at);
__e_acsl_assert_register_int(& __gen_e_acsl_assert_data, "\\result", 0,
                             __retres);
if (__gen_e_acsl_at <= __retres) {
  __e_acsl_assert_register_int(& __gen_e_acsl_assert_data, "\\old(y)", 0,
                              __gen_e_acsl_at_2);
  __e_acsl_assert_register_int(& __gen_e_acsl_assert_data, "\\result", 0,
                              __retres);
  __gen_e_acsl_and = __gen_e_acsl_at_2 <= __retres;
}
else __gen_e_acsl_and = 0;
...
__gen_e_acsl_and == 1 iff x <= \result && y <= \result
```

max.c

\$ frama-c -e-acsl max.c -then-last -print

Every call to max is replaced by a call to __gen_e_acsl_max.

E-ACSL Example 2

-With RTE-

```
int main(void) {  
    int x = 0xffff;  
    int y = 0xfff;  
    int z = x + y;  
    return 0;  
}
```

eacsl.c

\$ frama-c -rte eacsl.c -then -print

```
int main(void)  
{  
    int __retres;  
    int x = 0xffff;  
    int y = 0xfff;  
    /*@ assert rte: signed_overflow:  $-2147483648 \leq x + y$ ; */  
    /*@ assert rte: signed_overflow:  $x + y \leq 2147483647$ ; */  
    int z = x + y;  
    __retres = 0;  
    return __retres;  
}
```

E-ACSL Example 2

-With RTE+E-ACSL-

```
int main(void) {
  int x = 0xffff;
  int y = 0xffff;
  int z = x + y;
  return 0;
}
```

eacsl.c

\$ frama-c -rte eacsl.c -then -e-acsl -then-last -print

```
int main(void)
{
  int __retres;
  __e_acsl_memory_init((int *)0,(char **)0,8UL);
  int x = 0xffff;
  int y = 0xffff;
  {
    ...
    /*@ assert rte: signed_overflow: -9223372036854775808 ≤ x + (long)y; */
    /*@ assert rte: signed_overflow: x + (long)y ≤ 9223372036854775807; */
    __e_acsl_assert(x + (long)y ≤ 2147483647L,& __gen_e_acsl_assert_data);
    ...
    /*@ assert rte: signed_overflow: -9223372036854775808 ≤ x + (long)y; */
    /*@ assert rte: signed_overflow: x + (long)y ≤ 9223372036854775807; */
    __e_acsl_assert(-2147483648L ≤ x + (long)y,& __gen_e_acsl_assert_data_2);
    __e_acsl_assert_clean(& __gen_e_acsl_assert_data_2);
  }
  /*@ assert rte: signed_overflow: -2147483648 ≤ x + y; */
  /*@ assert rte: signed_overflow: x + y ≤ 2147483647; */
  int z = x + y;
  __retres = 0;
  __e_acsl_memory_clean();
  return __retres;
}
```

Limitations of E-ACSL

- Uninitialized values
 - Runtime error may not occur depending on the compiler
- Incomplete programs
- Recursive functions
- Variadic functions
- Function pointers

```
int main(void) {  
    int x;  
    /*@ assert x == 0; */  
    return 0;  
}
```

Test Cases Generation via PathCrawler

- Generate test inputs
- Cover all feasible execution paths
- Based on constraint resolution
- Try it online at <http://pathcrawler-online.com:8080/>

A Simple Example for PathCrawler

```
int foo(int x) {  
    pathcrawler_assert(x > 0);  
    return x + 1;  
}
```

simple.c

pathcrawler_assert(condition)

- May be used at any location in the program under test
- Will force the tool to generate test cases to cover both
 - the case condition is true, and
 - condition is false

A Simple Example for PathCrawler (cont'd)

Test Cases

- 1
- 2**

Path [Input values](#) [Output values](#) [Verdict](#) [Test driver](#) [Path predicate](#)

Path

simple.c:-4

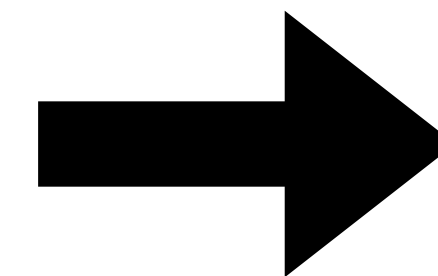
```
1 #include <stdlib.h>
2
3 int foo(int x) {
4 pathcrawler_assert(x > 0);
5 return x + 1;
6 }
7
```

All conditions fully covered Partial coverage No coverage

Program Slicing

- **Program slicing** computes a subset of program statements that may affect a given set of values called **slicing criterion**
- control dependency
- data dependency

```
...  
if (i <= j)  
    x = y * 2;  
else  
    y = y + 3;  
return x;
```



```
...  
if (i <= j)  
    x = y * 2;  
  
return x;
```

slicing criterion: x at the end of the program

Program Slicing

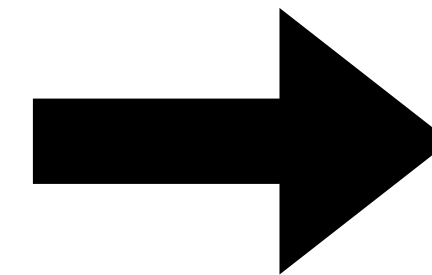
-Example 1-

```
int max(int m, int n) {
    if (m <= n) return n;
    else return m;
}

int dbl(int m) {
    return m * 2;
}

int f(void) {
    int m = 3, n = 5;
    int a = max(m, n);
    int b = dbl(m);
    /*@ assert b <= 10; */
    int c = b + 100;
    return c;
}

void main(void) { f(); ... }
```



```
/* Generated by Frama-C */
int dbl_slice_1(int m)
{
    int __retres;
    __retres = m * 2;
    return __retres;
}

void f_slice_1(void)
{
    int m = 3;
    int b = dbl_slice_1(m);
    /*@ assert b ≤ 10; */ ;
    return;
}

void main(void) { f_slice_1(); ... }
```

slicing-1.c

\$ frama-c slicing-1.c -slice-assert f -then-last -print

Slicing Criteria

-Code Observation-

- -slice-calls f1,...,fn: calls to functions f1,...,fn
- -slice-return f1,...,fn: returned values of functions f1,...,fn
- -slice-value v1,...,vn: left-values at the end of the entry function (specified by -main)
- -slice-wr v1,...,vn: write accesses to left-values
- -slice-rd v1,...,vn: read accesses to left-values
- -slice-pragma f1,...,fn: slicing pragmas in the code of functions f1,...,fn

Ref: <https://frama-c.com/fc-plugins/slicing.html>

Slicing Criteria

-Proving Properties-

- -slice-assert f_1, \dots, f_n : assertions of functions f_1, \dots, f_n
- -slice-loop-inv f_1, \dots, f_n : loop invariants of functions f_1, \dots, f_n
- -slice-loop-var f_1, \dots, f_n : loop variants of functions f_1, \dots, f_n
- -slice-threat f_1, \dots, f_n : threats (emitted by Eva) of functions f_1, \dots, f_n

Program Slicing

-Example 2: Case 1 of -slice-rd-

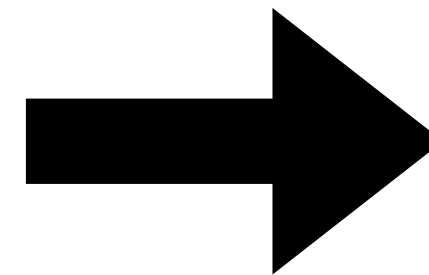
```
int max(int m, int n) { ... }

int dbl(int m) { ... }

int f(void) {
    int m = 3, n = 5;
    int a = max(m, n);
    int b = dbl(m);
    /*@ assert b <= 10; */
    int c = b + 100;
    return c;
}

void main(void) { f(); ... }
```

slicing-1.c



```
/* Generated by Frama-C */
void f(void)
{
    return;
}
```

\$ frama-c slicing-1.c -slice-rd c -main f -then-last -print

Program Slicing

-Example 3: Case 2 of -slice-rd-

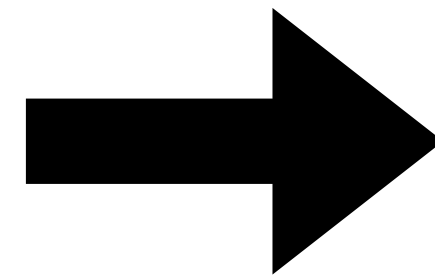
```
int max(int m, int n) { ... }

int dbl(int m) { ... }

int f(void) {
    int m = 3, n = 5;
    int a = max(m, n);
    int b = dbl(m);
    /*@ assert b <= 10; */
    int c = b + 100;
    return c + a;
}

void main(void) { f(); ... }
```

slicing-2.c



```
$ frama-c slicing-2.c -slice-rd c -main f -then-last -print
```


Program Slicing

-Example 3: Case 2 of -slice-rd-

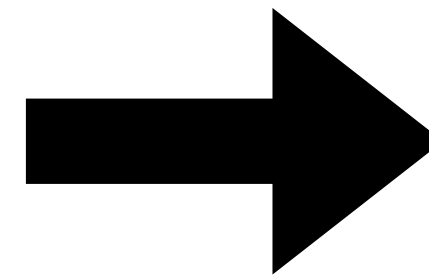
```
int max(int m, int n) { ... }

int dbl(int m) { ... }

int f(void) {
    int m = 3, n = 5;
    int a = max(m, n);
    int b = dbl(m);
    /*@ assert b <= 10; */
    int c = b + 100;
    return c + a;
}

void main(void) { f(); ... }
```

slicing-2.c



```
/* Generated by Frama-C */
int max_slice_1(int n)
{ ... }

int dbl_slice_1(int m)
{ ... }

void f(void)
{
    int __retres;
    int m = 3;
    int n = 5;
    int a = max_slice_1(n);
    int b = dbl_slice_1(m);
    /*@ assert b ≤ 10; */ ;
    int c = b + 100;
    __retres = c + a;
    return;
}
```

\$ frama-c slicing-2.c -slice-rd c -main f -then-last -print

Program Slicing

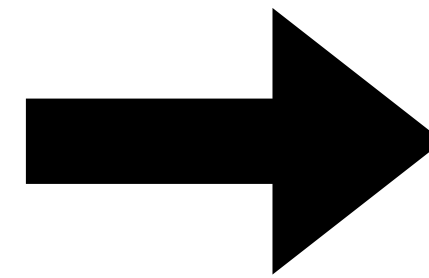
-Example 4: -slice-pragma-

```
int max(int m, int n) { ... }

int dbl(int m) { ... }

int f(void) {
    int m = 3, n = 5;
    int a = max(m, n);
    /*@ slice pragma expr a; */
    /*@ slice pragma stmt; */
    int b = dbl(m);
    /*@ assert b <= 10; */
    int c = b + 100;
    return c + a;
}

void main(void) { f(); ... }
```



slicing-3.c

\$ frama-c slicing-3.c -slice-pragma f -main f -then-last -print

Program Slicing

-Example 4: -slice-pragma-

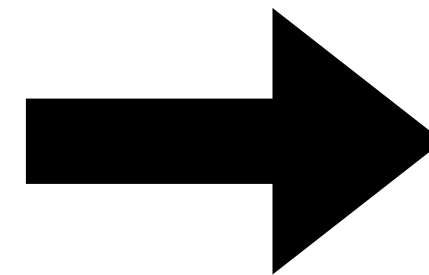
```
int max(int m, int n) { ... }

int dbl(int m) { ... }

int f(void) {
    int m = 3, n = 5;
    int a = max(m, n);
    /*@ slice pragma expr a; */
    /*@ slice pragma stmt; */
    int b = dbl(m);
    /*@ assert b <= 10; */
    int c = b + 100;
    return c + a;
}

void main(void) { f(); ... }
```

slicing-3.c



```
/* Generated by Frama-C */
int max_slice_1(int n)
{ ... }

int dbl_slice_1(int m)
{ ... }

void f(void)
{
    int __retres;
    int m = 3;
    int n = 5;
    int a = max_slice_1(n);
    /*@ slice pragma expr a; */ ;
    /*@ slice pragma stmt; */
    int b = dbl_slice_1(m);
    /*@ assert b ≤ 10; */ ;
    return;
}
```

\$ frama-c slicing-3.c -slice-pragma f -main f -then-last -print

Deductive Verification via WP

- Based on weakest-precondition calculus
- Relies on external automated provers and proof assistants
- Provers are invoked via Why3 (<http://why3.lri.fr>)
 - Alt-Ergo
 - CVC4
 - Gappa
 - Princess
 - Vampire
 - Z3
 - Coq
 - PVS
 - Isabelle/HOL

After installation of why3 and external provers, run command ``why3 config detect`` to detect available provers.

WP Example 1

```
/*@  
  @ ensures \result == x + y;  
  @ assigns \nothing;  
  */  
int add(int x, int y) {  
  return x + y;  
}
```

add.c

```
$ frama-c -wp add.c -then -report
```

```
[kernel] Parsing add.c (with preprocessing)  
[wp] Warning: Missing RTE guards  
[wp] 2 goals scheduled  
[wp] [Cache] not used  
[wp] Proved goals:  2 / 2  
  Qed:          2  
[report] Computing properties status...
```

```
-----  
--- Properties of Function 'add'  
-----
```

```
[ Valid ] Post-condition (file add.c, line 2)  
          by Wp.typed.  
[ Valid ] Assigns nothing  
          by Wp.typed.  
[ Valid ] Default behavior  
          by Frama-C kernel.
```

...

WP Example 2

-With RTE-

```
/*@
  @ ensures \result == x + y;
  @ assigns \nothing;
 */
int add(int x, int y) {
  return x + y;
}
```

add.c

```
$ frama-c -wp -wp-rte add.c -then -report
```

Refine the specification such that the absence of runtime errors can be proven

```
[kernel] Parsing add.c (with preprocessing)
[rte:annot] annotating function add
[wp] 4 goals scheduled
[wp] [Timeout] typed_add_assert_rte_signed_overflow_2 (Alt-Ergo) (Cached)
[wp] [Timeout] typed_add_assert_rte_signed_overflow (Alt-Ergo) (Cached)
[wp] [Cache] updated:2
[wp] Proved goals: 2 / 4
  Qed:      2
  Timeout:  2
[report] Computing properties status...
...
[ Partial ] Post-condition (file add.c, line 2)
  By Wp.typed, with pending:
    - Assertion 'rte,signed_overflow' (file add.c, line 6)
    - Assertion 'rte,signed_overflow' (file add.c, line 6)
...
[ - ] Assertion 'rte,signed_overflow' (file add.c, line 6)
      tried with Wp.typed.
[ - ] Assertion 'rte,signed_overflow' (file add.c, line 6)
      tried with Wp.typed.
...
37
```

WP Example 3

```
/*@ requires \valid(a) && \valid(b);
   @ ensures *a == \old(*b) && *b == \old(*a);
   @ assigns *a, *b;
   @*/
void swap(int *a, int *b)
{
    int tmp = *a;
    *a = *b;
    *b = tmp;
}

void order3(int *a, int *b, int *c) {
    if (*a > *b) swap(a, b);
    if (*a > *c) swap(a, c);
    if (*b > *c) swap(b, c);
}
```

order3.c

Write a specification for order3

WP Example 3

```
/*@ requires \valid(a) && \valid(b);  
@ ensures *a == \old(*b) && *b == \old(*a);  
@ assigns *a,  
@*/
```

```
void swap(int *  
{  
    int tmp = *a;  
    *a = *b;  
    *b = tmp;  
}
```

```
void order3(int  
    if (*a > *b)  
    if (*a > *c)  
    if (*b > *c) swap(b, c);  
}
```

```
/*@  
@ requires \valid(a) && \valid(b) && \valid(c) && \separated(a, b, c);  
@ ensures *a <= *b <= *c;  
@ ensures { *a, *b, *c } == { \old(*a), \old(*b), \old(*c) };  
@ assigns *a, *b, *c;  
@*/
```

```
void order3(int *a, int *b, int *c) {  
    if (*a > *b) swap(a, b);  
    if (*a > *c) swap(a, c);  
    if (*b > *c) swap(b, c);  
}
```

sol/order3-annotated-1.c

order3.c

WP Example 3

-Additional Assertions-

```
/*@ requires \valid(a) && \valid(b);
   @ ensures *a == \old(*b) && *b == \old(*a);
   @ assigns *a, *b;
   @*/
void swap(int *a, int *b)
{
    int tmp = *a;
    *a = *b;
    *b = tmp;
}

void order3(int *a, int *b, int *c) {
    if (*a > *b) swap(a, b);
    if (*a > *c) swap(a, c);
    if (*b > *c) swap(b, c);
}
```

sol/order3-annotated-2.c

```
void test() {
    int a1 = 5, b1 = 3, c1 = 4;

    order3(&a1, &b1, &c1);
    //@ assert a1 == 3 && b1 == 4 && c1 == 5;

    int a2 = 2, b2 = 2, c2 = 2;
    order3(&a2, &b2, &c2);
    //@ assert a2 == 2 && b2 == 2 && c2 == 2;

    int a3 = 4, b3 = 3, c3 = 4;
    order3(&a3, &b3, &c3);
    //@ assert a3 == 3 && b3 == 4 && c3 == 4;

    int a4 = 4, b4 = 5, c4 = 4;
    order3(&a4, &b4, &c4);
    //@ assert a4 == 4 && b4 == 4 && c4 == 5;
}
```

WP Example 3

-Additional Assertions-

```
/*@ requires \valid(a) && \valid(b);
   @ ensures *a == \old(*b) && *b == \old(*a);
   @ assigns *a, *b;
   @*/
void swap(int *a, int *b)
{
    int tmp = *a;
    *a = *b;
    *b = tmp;
}

void order3(int *a, int *b, int *c) {
    if (*a > *b) swap(a, b);
    if (*a > *c) swap(a, c);
    if (*b > *c) swap(b, c);
}
```

With the previous annotation

sol/order3-annotated-2.c

```
void test() {
    int a1 = 5, b1 = 3, c1 = 4;
    order3(&a1, &b1, &c1);
    ○ //@ assert a1 == 3 && b1 == 4 && c1 == 5;

    int a2 = 2, b2 = 2, c2 = 2;
    order3(&a2, &b2, &c2);
    ○ //@ assert a2 == 2 && b2 == 2 && c2 == 2;

    int a3 = 4, b3 = 3, c3 = 4;
    order3(&a3, &b3, &c3);
    ✗ //@ assert a3 == 3 && b3 == 4 && c3 == 4;

    int a4 = 4, b4 = 5, c4 = 4;
    order3(&a4, &b4, &c4);
    ✗ //@ assert a4 == 4 && b4 == 4 && c4 == 5;
}
```

Write a specification for order3 such that all assertions are verified

WP Example 3

-Refined Annotations I-

```
/*@
  @ requires \valid(a) && \valid(b) && \valid(c) && \separated(a, b, c);
  @ ensures *a <= *b <= *c;
  @ ensures { *a, *b, *c } == { \old(*a), \old(*b), \old(*c) };
  @ ensures (\old(*a) == \old(*b)) ==>
            (*a == *b == \old(*a) || *b == *c == \old(*a) || *c == *a == \old(*a));
  @ ensures (\old(*b) == \old(*c)) ==>
            (*a == *b == \old(*b) || *b == *c == \old(*b) || *c == *a == \old(*b));
  @ ensures (\old(*c) == \old(*a)) ==>
            (*a == *b == \old(*c) || *b == *c == \old(*c) || *c == *a == \old(*c));
  @ assigns *a, *b, *c;
  @*/
void order3(int *a, int *b, int *c) {
  if (*a > *b) swap(a, b);
  if (*a > *c) swap(a, c);
  if (*b > *c) swap(b, c);
}
```

sol/order3-annotated-3.c

WP Example 3

-Refined Annotations II-

```
/*@
@ requires \valid(a) && \valid(b) && \valid(c) && \separated(a, b, c);
@ ensures *a <= *b <= *c;
@ ensures { *a, *b, *c } == { \old(*a), \old(*b), \old(*c) };
@ ensures \forall int* x, int* y;
        \subset({ x, y }, { a, b, c }) && \separated(x, y) && \old(*x) == \old(*y) ==>
        \exists int* u, int* v;
        \subset({ u, v }, { a, b, c }) && \separated(u, v) && *u == *v == \old(*x);
@ assigns *a, *b, *c;
@*/
void order3(int *a, int *b, int *c) {
if (*a > *b) swap(a, b);
if (*a > *c) swap(a, c);
if (*b > *c) swap(b, c);
}
```

sol/order3-annotated-5.c

WP Exercise

```
#include <limits.h>

/*@
 @ requires 0 <= x <= INT_MAX / 2;
 @ assigns \nothing;
 @ ensures \result == 2 * x;
 @*/
int times2 (int x) {
    int r = 0 ;
    /*@
     @ loop invariant ...;
     @ loop assigns ...;
     @ loop variant ...;
     @*/
    while (x > 0) {
        r += 2;
        x --;
    }
    return r;
}
```

Deductive Verification with Interactive Prover

- For proof obligations that cannot be discharged by automatic provers, an interactive prover such as Coq can be used
- We show how to use interactive provers in the following examples

Prover: Script

The screenshot shows the Frama-C GUI with the following components:

- File Editor:** Displays two lemmas:
 - `lemma Zmul_le_mono_nonneg_l: $\forall \mathbb{Z} x, \mathbb{Z} y, \mathbb{Z} z; 0 \leq x \Rightarrow y \leq z \Rightarrow x * y \leq x * z;$`
 - `lemma Zadd_le_mul: $\forall \mathbb{Z} x, \mathbb{Z} y; 2 \leq x \Rightarrow 2 \leq y \Rightarrow x + y \leq x * y;$`
- WP Goals Table:** A table with columns: Module, Goal, Model, Qed, Script, and Alt-Ergo 2.4.2.

Module	Goal	Model	Qed	Script	Alt-Ergo 2.4.2
Axiomatics	Lemma 'Zadd_le_mul'	Typed	-	-	
Axiomatics	Lemma 'Zmul_le_mono_nonneg_l'	Typed	-	-	
- Left Panel:** Contains settings for WP (2 time, 4 proc), Slicing (Enable, Libraries), Occurrence (Read, Write checked), and Metrics.

Prover: Script

The screenshot displays the Frama-C interface with two overlapping windows. The background window shows the 'WP Goals' tab with a goal list. The foreground window shows the script editor for 'ex_script.c'.

Script Editor Content:

```
/*@
lemma Zmul_le_mono_nonneg_l:
  ∀ ℤ x, ℤ y, ℤ z; 0 ≤ x ⇒ y ≤ z ⇒ x * y ≤ x * z;
*/
/*@
lemma Zadd_le_mul: ∀ ℤ x, ℤ y; 2 ≤ x ⇒ 2 ≤ y ⇒ x + y ≤ x * y;
*/
```

Goal List Content:

```
script '.frama-c/wp/script/lemma_Zmul_le_mono_nonneg_l.json' (not created)
-----
No Script
-----
Lemma Lemma 'Zmul_le_mono_nonneg_l':
Assume { Have: 0 <= x_0. Have: y_0 <= z_0. }
Prove: (x_0 * y_0) <= (x_0 * z_0).

Goal id: typed_lemma_Zmul_le_mono_nonneg_l
Short id: lemma_Zmul_le_mono_nonneg_l
-----
Driver Alt-Ergo 2.4.2: Timeout (2s) (cached)
```

Tactics Panel:

- Alt-Ergo 2.4.2 (?)
- Strategies
- Cut
- Filter

Red annotations in the image point to the 'Current goal' (the goal list) and 'Tactics' (the tactics panel).

Script Prover

-Example-

```
/*@
 @ lemma Zmul_le_mono_nonneg_l :
 @     \forall integer x, y, z;
 @     0 <= x ==> y <= z ==> x * y <= x * z;
 @
 @ lemma Zadd_le_mul :
 @     \forall integer x, y;
 @     2 <= x ==> 2 <= y ==> x + y <= x * y;
 @*/

/*@
 @ requires 2 <= x;
 @ requires 2 <= y;
 @ requires x * (x * y) <= INT_MAX;
 @ ensures x * (x + y) <= x * (x * y);
 @ assigns \nothing;
 @*/
void foo(int x, int y) {
}
```

ex_script.c

Script Prover

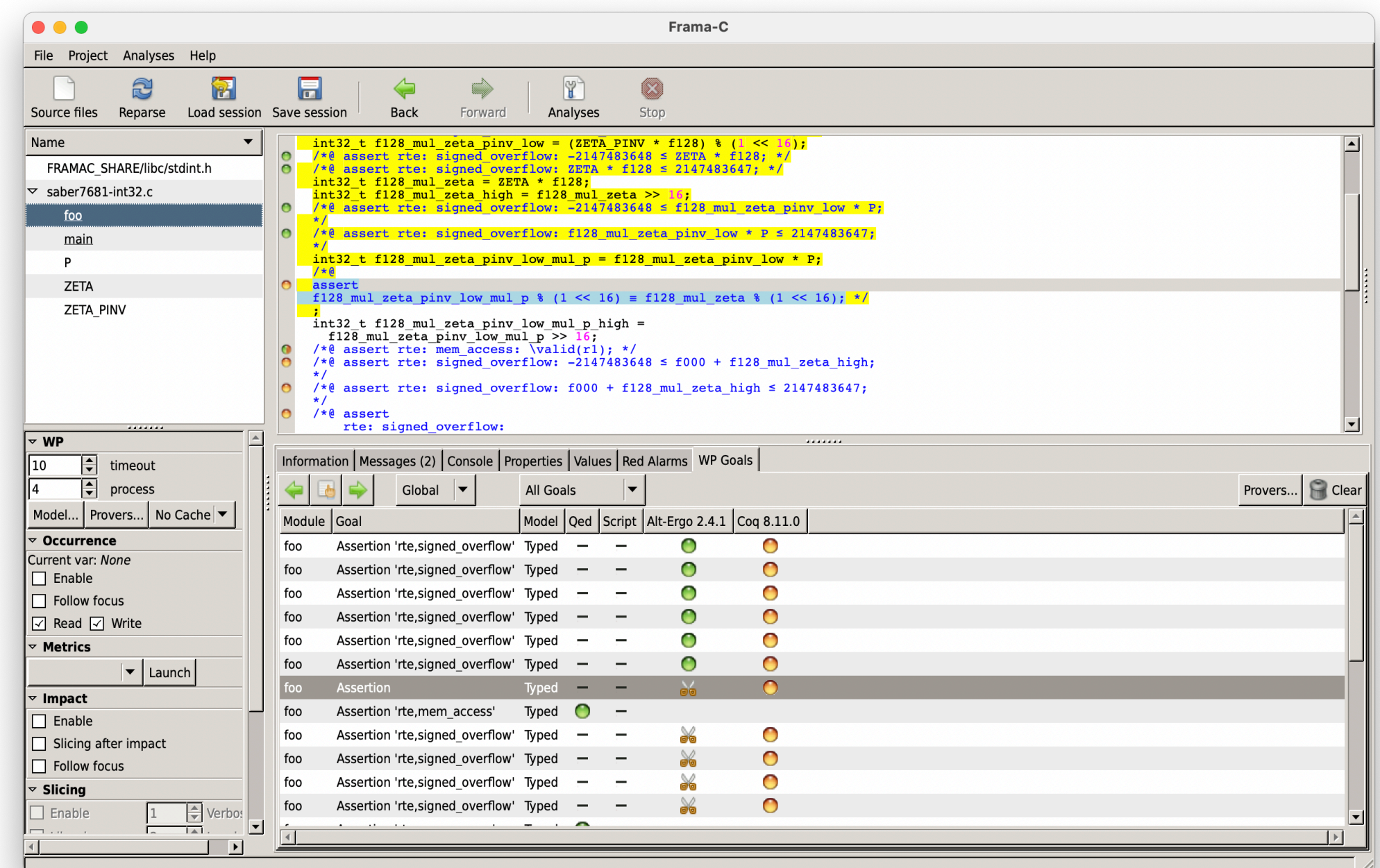
-Applying Tactics-

- Zmul_le_mono_nonneg_l:
 - Apply induction on x
- Zadd_le_mul
 - Apply induction on x
 - Case analysis on \leq
- Scripts can be saved and replayed with `tip` added to `-wp-prover`

Prover: Coq

- Run the following command to invoke Frama-C
`$ frama-c-gui -wp -wp-rte -wp-prover alt-ergo,coq EXAMPLE.c`
- Double click the orange circle of the assertion on the Coq column to edit the Coq proof script

- unknown
- surely valid
- surely invalid
- valid under hypothesis
- invalid under hypothesis



Field Operations

-Annotated C Code-

```
const int32_t P = 7681;
const int32_t ZETA = 3777;
const int32_t ZETA_PINV = 28865;

/*@
 @ requires \valid(r1) && \valid(r2);
 @ requires \separated(r1, r2, &P, &ZETA, &ZETA_PINV);
 @ requires (-4096 < f000 < 4096);
 @ requires (-4096 < f128 < 4096);
 @ assigns *r1, *r2;
 @*/
void foo(const int32_t f000, const int32_t f128, int32_t *r1, int32_t *r2) {
    int32_t f128_mul_zeta_pinv_low = (ZETA_PINV * f128) % (1 << 16);
    int32_t f128_mul_zeta = ZETA * f128;
    int32_t f128_mul_zeta_high = f128_mul_zeta >> 16;
    int32_t f128_mul_zeta_pinv_low_mul_p = f128_mul_zeta_pinv_low * P;
    //@ assert f128_mul_zeta_pinv_low_mul_p % (1 << 16) == f128_mul_zeta % (1 << 16);
    int32_t f128_mul_zeta_pinv_low_mul_p_high = f128_mul_zeta_pinv_low_mul_p >> 16;
    *r1 = f000 + f128_mul_zeta_high - f128_mul_zeta_pinv_low_mul_p_high;
    *r2 = f000 - f128_mul_zeta_high + f128_mul_zeta_pinv_low_mul_p_high;
}
```

saber7681-int32.c

alt-ergo fails to prove the assertion

Field Operations

-Proof Obligations-

```
/*@
  @ requires \valid(r1) && \valid(r2);
  @ requires \separated(r1, r2, &P, &ZETA, &ZETA_PINV);
  @ requires (-4096 < f000 < 4096);
  @ requires (-4096 < f128 < 4096);
  @ assigns *r1, *r2;
  @*/
void foo(const int32_t f000, const int32_t f128, int32_t *r1, int32_t *r2) {
  // (((ZETA_PINV * f128) % (1 << 16)) * P) % (1 << 16) == (ZETA * f128) % (1 << 16)
  int32_t f128_mul_zeta_pinv_low = (ZETA_PINV * f128) % (1 << 16);
  // (f128_mul_zeta_pinv_low * P) % (1 << 16) == (ZETA * f128) % (1 << 16)
  int32_t f128_mul_zeta = ZETA * f128;
  // (f128_mul_zeta_pinv_low * P) % (1 << 16) == f128_mul_zeta % (1 << 16)
  int32_t f128_mul_zeta_high = f128_mul_zeta >> 16;
  // (f128_mul_zeta_pinv_low * P) % (1 << 16) == f128_mul_zeta % (1 << 16)
  int32_t f128_mul_zeta_pinv_low_mul_p = f128_mul_zeta_pinv_low * P;
  //@ assert f128_mul_zeta_pinv_low_mul_p % (1 << 16) == f128_mul_zeta % (1 << 16);
  ...
}
```

$\backslash\text{valid}(r1) \ \&\& \ \backslash\text{valid}(r2) \ \rightarrow \ \backslash\text{separated}(r1, r2, \&P, \&ZETA, \&ZETA_PINV) \ \rightarrow \ (-4096 < f000 < 4096) \ \rightarrow \ (-4096 < f128 < 4096) \ \rightarrow$
 $((ZETA_PINV * f128) \% (1 \ll 16)) * P \% (1 \ll 16) == (ZETA * f128) \% (1 \ll 16)$

Field Operations

-Prove by Hand-

```
((ZETA_PINV * f128) % (1 << 16)) * P) % (1 << 16)
= ((28865 * f128) % 65536) * 7681) % 65536
= (28865 * f128) * 7681) % 65536           # ((a%n) * b)%n = (a * b)%n
= (7681 * (28865 * f128)) % 65536           # a * b = b * a
= ((7681 * 28865) * f128) % 65536           # a * (b * c) = (a * b) * c
= ((7681 * 28865) % 65536 * f128) % 65536   # ((a%n) * b)%n = (a * b)%n
= (3777 * f128) % 65536
= (ZETA * f128) % (1 << 16)
```

```
const int32_t P = 7681;
const int32_t ZETA = 3777;
const int32_t ZETA_PINV = 28865;
```

Field Operations

-Prove Goals using Coq-

- Assertion
 - `.frama-c/wp/interactive/foo_assert.v`
 - Print definitions
 - Search for lemmas
 - Basic tactics

Multiplication by Addition

-Annotated C Code-

```
/*@
 @ requires INT_MIN <= x * y <= INT_MAX;
 @ ensures \result == x * y;
 @*/
int mul(int x, int y) {
    int r = 0;
    /*@
     @ loop assigns r, y;
     @ loop invariant r + x * y == \at(x, Pre) * \at(y, Pre);
     @ loop variant \abs(y);
     @*/
    while (y != 0) {
        if (0 < y) { r += x; y -= 1; }
        else      { r -= x; y += 1; }
    }
    return r;
}
```

mul_by_add.c

Multiplication by Addition

-Prove Goals using Coq-

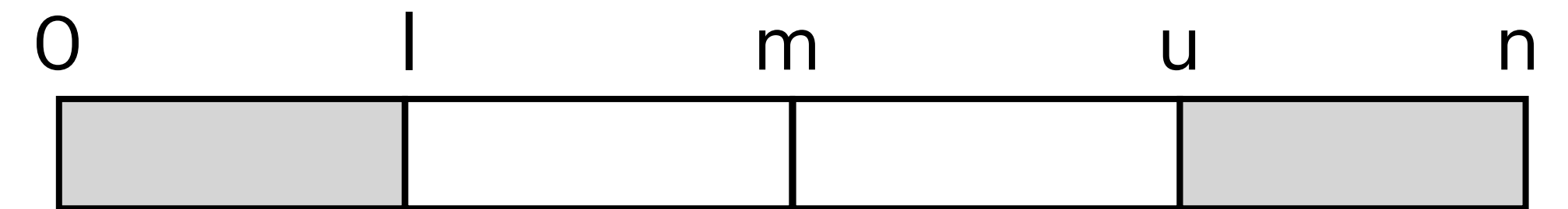
- Invariant (preserved)
 - `.frama-c/wp/interactive/mul_loop_invariant_preserved.v`
 - Basic tactics
 - Proof automation
- Loop variant at loop (decrease)
 - `.frama-c/wp/interactive/mul_loop_variant_decrease.v`
 - Apply lemmas

Binary Search

-C Code-

```
int binary_search(long t[], int n, long v) {
    int l = 0, u = n - 1;
    while (l <= u) {
        int m = (l + u) / 2;
        if (t[m] < v)      l = m + 1;
        else if (t[m] > v) u = m - 1;
        else               return m;
    }
    return -1;
}
```

binary_search.c



Source: <http://proval.lri.fr/gallery/BinarySearchACSL.en.html> (invalid now)

Binary Search

-Function Contract-

```
/*@ requires 0 <= n <= (INT_MAX / 2) && \valid(t + (0..n-1));
   @ ensures -1 <= \result < n;
   @ assigns \nothing;
   @ behavior success:
   @   ensures \result >= 0 ==> t[\result] == v;
   @ behavior failure:
   @   assumes sorted(t,0,n-1);
   @   ensures \result == -1 ==>
   @     \forall integer k; 0 <= k < n ==> t[k] != v;
   @*/

int binary_search(long t[], int n, long v) {
    int l = 0, u = n - 1;
    while (l <= u) {
        int m = (l + u) / 2;
        if (t[m] < v) l = m + 1;
        else if (t[m] > v) u = m - 1;
        else return m;
    }
    return -1;
}
```

Binary Search

-Loop Annotations-

```
/*@ loop invariant 0 <= l <= u + 1 <= n;  
  @ loop assigns l, u;  
  @ for failure:  
  @   loop invariant  
  @   \forall integer k;  
  @   0 <= k < n && t[k] == v ==> l <= k <= u;  
  @ loop variant u-l;  
@*/
```

```
int binary_search(long t[], int n, long v) {  
    int l = 0, u = n - 1;  
    while (l <= u) {  
        int m = (l + u) / 2;  
        if (t[m] < v) l = m + 1;  
        else if (t[m] > v) u = m - 1;  
        else return m;  
    }  
    return -1;  
}
```

Binary Search

-Prove Goals using Coq-

- Invariant (preserved)
 - Contradiction
 - Focus mode
- Loop variant at loop (decrease)
- Post-condition
- Post-condition for `failure`
- Invariant for `failure` (preserved)

Nistonacci Numbers

-Axiomatic Definition-

$$\text{nist}(n) = \begin{cases} n & \text{if } n < 2 \\ \text{nist}(n - 2) + 2 * \text{nist}(n - 1) & \text{otherwise} \end{cases}$$

```
/*@  
@ axiomatic Nist {  
@   logic integer nist(integer n);  
@   axiom nist1 : \forall integer n; n < 2 ==> nist(n) == n;  
@   axiom nist2 : \forall integer n; !(n < 2) ==> nist(n) == nist(n - 2) + 2 * nist(n - 1);  
@ }  
@*/
```

nistonacci.c

Nistonacci Numbers

-Goal-

```
/*@  
  @ requires 0 <= n < m;  
  @ ensures n < nist(m);  
  @ assigns \nothing;  
  @*/  
void foo(int n, int m) {  
  ...  
}
```

nistonacci.c

alt-ergo fails to prove the postcondition

Nistonacci Numbers

-Lemma-

```
//@ lemma nist_geN : \forall integer n; 0 <= n ==> n <= nist(n);

/*@
  @ requires 0 <= n < m;
  @ ensures n < nist(m);
  @ assigns \nothing;
  @*/
void foo(int n, int m) {
  ...
}
```

nistonacci-lemma.c

alt-ergo proves the postcondition but fails to prove the lemma

Nistonacci Numbers

-Implement nist-

```
/*@
 @ requires 0 <= n;
 @ ensures n <= \result;
 @ assigns \nothing;
 @*/
int nist_impl(int n) {
  int x = 0, y = 1, i = 0;
  /*@
   @ loop invariant 0 <= i <= n;
   @ loop invariant x == nist(i);
   @ loop invariant y == nist(i + 1);
   @ loop assigns x, y, i;
   @*/
  for (i = 0; i < n; i++) {
    int tmp = x;
    x = y;
    y = tmp + 2 * y;
  }
  return x;
}
```

nistonacci-impl.c

Nistonacci Numbers

-Prove Goals using Coq-

- Invariant (preserved) ($y = \text{nist}(n + 1)$)
 - Order of operands
 - Replace terms
- Post-condition
 - Induction

Nistonacci Numbers

-Prove Postcondition by Alt-ergo-

- What can be added to the annotations so that alt-ergo can prove the postcondition ($n \leq \text{\result}$)?

```
/*@
 @ requires 0 <= n;
 @ ensures n <= \result;
 @ ensures \result == nist(n);
 @ assigns \nothing;
 */
int nist_impl(int n) {
  int x = 0, y = 1, i = 0;
  /*@
   @ loop invariant 0 <= i <= n;
   @ loop invariant x == nist(i);
   @ loop invariant y == nist(i + 1);
   @ loop assigns x, y, i;
   */
  for (i = 0; i < n; i++) {
    int tmp = x;
    x = y;
    y = tmp + 2 * y;
  }
  return x;
}
```

Nistonacci Numbers

-Lemma Function-

```
/*@ ghost
/@
@ requires 0 <= n;
@ ensures n <= \result;
@ ensures \result == nist(n);
@ assigns \nothing;
@/
int nist_impl(int n) {
    ...
}
@*/

/*@
@ requires 0 <= n < m;
@ ensures n < nist(m);
@ assigns \nothing;
@*/
void foo(int n, int m) {
    //@ ghost nist_impl(m);
}
```

Nistonacci Numbers

-Simpler Lemma Function-

```
/*@ ghost
/@
@ requires 0 <= n;
@ ensures n <= nist(n);
@ assigns \nothing;
@/
void nist_geN(int n) {
    if (n >= 2) {
        nist_geN(n-1);
        nist_geN(n-2);
    }
    return;
}
@*/
```

nistonacci-rec.c

Inconsistent Annotations

```
/*@ logic integer last0(integer n) = n%10 == 0 ? 1 + last0(n / 10) : 0; */

/*@
  ensures \false;
  assigns \nothing;
 */
int foo(void) {
  /*@ assert last0(0) == 1; */
  return 0;
}
```

Output:

```
...
[wp] Proved goals: 3 / 3
Qed: 1
Alt-Ergo 2.4.2: 2 (5ms)
```

inconsistent1.c

Summary

- Frama-C is a powerful and flexible tool for deductive program verification
- There are still the following challenges:
 - Write a correct specification
 - Write a strong enough loop invariant
 - Analyze proof failures

Reference: Nikolai Kosmatov, Virgile Prevosto, and Julien Signoles. A Lesson on Proof of Programs with Frama-C. Invited Tutorial Paper. International Conference on Tests and Proofs. 2013.